A Fuzzy PID Control Method for the Underwater Spherical Robot

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Abstract – The motion control of underwater spherical robot is a complicated process, which has the characteristics of high inertia and non-linearity. There are many influencing factors for the underwater spherical robot motion such as ambient temperature and water current, so it is difficult to obtain the real-time kinematic model. Therefore, it is hard for traditional PID to achieve stable motion control of the underwater spherical robot. In this paper, the actual motion control of underwater spherical robot was realized that used fuzzy PID control method. Compared with traditional PID for the underwater spherical robot, fuzzy PID has some advantages, such as good robustness and good dynamic performance. To demonstrate that the fuzzy PID was more suitable to our underwater spherical robot, we carried out some real time experiments. Comparison experimental results demonstrated that the fuzzy PID control method has better dynamic performance than the traditional PID.

Index Terms – Underwater Motion Control; Underwater Spherical Robot; Fuzzy PID Algorithm;

I. INTRODUCTION

Land resources are over-collected, so the land resources are increasingly scarce. As we all know, the ocean area accounts for 71% of the total area of the earth. Therefore, the rational use of marine resources and the environment has attracted the attention of researchers. In order to satisfy the urgent need for marine scientific research and military missions. Underwater spherical robot was developed by us, which has high mobility, high concealment, high adaptability and other advantages. Currently, researchers study underwater autonomous robots, most of them designed underwater autonomous robots by using traditional torpedo shape. Generally, this type of robots have many disadvantages, such as big shape and using propeller as power. Therefore, these shortcomings caused them to have high noise, low concealment, etc. They are difficult to finish the detection and sampling tasks in a variety of extreme environments [1]-[2], such as the detection of submarine volcano and mineral collection in seabed rock seam.

The study of underwater spherical robots began in the early 1990s, and the University of Hawaii designed a spherical underwater robot: Omni-Directional Intelligent Navigator (ODIN). ODIN is mainly used to environmental monitoring and underwater operation. ODIN has eight thrusters, sonar sensor, pressure sensor and inertial navigation system [3]-[4]. With the successful design of ODIN, many researchers began to carry out various research work for the underwater robots, and the researchers obtained a series of research achievement of underwater robot.

The motion control of underwater robot is a main technology of underwater robot. The stability control of underwater robot is very important. The control of underwater robots include a lot of aspects. Like machine vision, path programming, trajectory tracking, information fusion, environment modeling, fluid mechanics analysis, fault diagnosis, obstacle avoidance, navigation, communication, etc. Underwater spherical robot is not only a strongly nonlinear system, but also a multi-input/multi-output system. Meanwhile, underwater robot can be susceptible to the uncertainty of ocean current. Therefore, it is difficult to obtain stable motion control in the underwater environment. When researchers selected some traditional methods such as traditional PID control algorithm to design the underwater robot controller, they cannot obtained the expected control due to the anti-disturbance ability is not strong enough. The researchers have developed a lot of new methods, but some of the practical application of control methods were difficult to achieve. Most of the underwater robot motion control methods were still in the simulation stage, so it is necessary to develop new ways to solve these problems in the practical application. At present, the control algorithms of underwater robot have the following method: PID control, adaptive control, fuzzy control, sliding mode control, neural network control, robust control [5], and the combination of several control methods, etc.

Compare with the research [6], they proposed a motion control of amphibious robot based on fuzzy PID. But it just only used the simulation to compare the traditional PID and fuzzy PID. It did not finish the actual robot experiment, and only analysis the advantages of fuzzy PID in the theoretical. So the membership function and the PID parameters are different from the actual experiments.

However, in this paper, we focus on actual underwater motion control experiments of amphibious robot that is using fuzzy PID control method, not just the simulation, and the
member function and the PID parameters had been selected more reasonable.

The structure of this paper is organized as follows. Section II introduces the structure and some dynamic equations of the amphibious spherical robot, also with some thruster’s measure experiments. Traditional PID and fuzzy PID control method are introduced in Section III, and the experimental results are provided in Section IV. Finally, Section V presents some conclusions and future work.

II. RELATED WORKS

A. Amphibious spherical robot

In previous researches, the amphibious spherical robot was developed with high mobility and high hidden [7-8]. The application of a wide range of prospects, its application areas involving industry, fisheries, exploration, military, etc. The robot consists of a hemispherical body and four mechanical legs. As shown in Fig.1, the direction of the red line is the forward direction of the robot. The robot was equipped with a control system and a drive circuit in the upper hemisphere, and the robot has four two degrees of freedom mechanical legs in the lower hemisphere [9-12]. Each mechanical leg contains a water-jet thruster and two waterproof servo steering gears. Fixed in the horizontal and vertical bracket. The robot total diameter was 35 cm, and its weight in air was about 5.5 kg.

![Fig.1 The amphibious spherical robot](image)

The amphibious spherical robot have two model: the land mode and the underwater mode. The robot walked with four legs in the land mode, and it could drive with four water-jet thrusters in the underwater mode. The two mode as shown as in Fig.2, and this paper mainly studied the underwater motion control mode of robot.

![Fig.2 The motion mode of the amphibious spherical robot](image)

B. Dynamics equations of underwater spherical robot

In order to achieve a more effective control strategy, modeling of the underwater spherical robot is important. The generalized position and velocity are defined in six degrees of freedom (6-DOF) [13], which are usually defined as:

$$v = [u, v, w, p, q, r]^T \in \mathbb{R}^6$$  \hspace{1cm} (1)

$$\eta = [x, y, z, \phi, \theta, \psi]^T \in \mathbb{R}^3 \times S^3$$  \hspace{1cm} (2)

$$\omega = [p, q, r]^T \in \mathbb{R}^3$$  \hspace{1cm} (3)

$$\Theta = [\phi, \theta, \psi]^T \in S^3$$  \hspace{1cm} (4)

where $\mathbb{R}^3$ is n-dimensional Euclidean space, $S^3$ is a three-dimensional torus. When modeling the movement of a six-degree-of-freedom underwater robot, by two reference coordinate systems and using the vector defined in equation (1) to (4) were used to describe the information of position, direction, velocity, angular velocity, etc.

In order to calculate the position and direction of the robot. It’s necessary to know the line acceleration and angular acceleration of the robot. It’s clear that these accelerations are determined by the forces acting on the robot. So the dynamics of the robot can be divided into two parts: rigid body and torque, hydrodynamic and torque [14].

Firstly, rigid body and torque satisfy the following equation:

$$M_{bb} \ddot{v} + C_{bb}(v)v = \tau_m$$  \hspace{1cm} (5)

where: $M_{bb}$ is the robot inertia matrix, $M_A$ is the added mass inertia matrix, $C_{bb}(v)$ is Coriolis of robot, $\tau_m$ includes the total hydrodynamic force and torque including the load and controls the propulsion and torque.

Secondly, hydrodynamic and torque satisfy the following equation:

$$\tau_m = -M_A \ddot{v} - C_A(v)v - (D_l + D_q(v))v - g(\Theta) + \tau$$  \hspace{1cm} (6)

where $C_A(v)$ is Coriolis of added mass, $D_l$ is the linear damping matrix, $D_q$ is the nonlinear damping matrix, $g(\Theta)$ is the restoring force and moment vector, $\tau$ is control vector.

Finally, substituting equation (5) into equation (6). The total underwater spherical robot dynamics equation can be expressed as:

$$(M_{bb} + M_A) \ddot{v} + (C_{bb}(v) + C_A(v))v + (D_l + D_q(v))v + g(\Theta) = \tau$$  \hspace{1cm} (7)

In order to simplify the dynamics of underwater spherical robot model, the dynamics of the underwater spherical robot are declared as follows:

(1) The velocity of underwater spherical robot is less than 1m/s;

(2) During all experiments, the underwater spherical robot always hold in a horizontal attitude;

(3) The x and y directions of the underwater spherical robot have the same dynamic characteristics on the xy plane.

(4) The degree of freedom of the underwater spherical robot can be decoupled [15];

As the underwater spherical robot is considered to be symmetrically distributed, and the robot is moving at low velocity, and the decoupling of the freedom degree of the robot is well founded. Decoupling means that the Coriolis...
force and the centripetal force become negligible and can be eliminated from the dynamics model. Therefore, simplified dynamics model of the underwater spherical robot can be obtained:

\[(M_{RB} + M_a)v^2 + (D_v + D_y)v + g(\Theta) = \tau\]  \(\text{(8)}\)

The specific dynamics model of the underwater spherical robot in the XY plane can be expressed as:

\[\begin{bmatrix}
9.408 & 0 & 0 \\
0 & 9.408 & 0 \\
0 & 0 & 0.0826
\end{bmatrix}
+ \begin{bmatrix}
10.3 & 0 & 0 \\
0 & 10.3 & 0 \\
0 & 0 & 0.065
\end{bmatrix}
\begin{bmatrix}v \\ \dot{v} \end{bmatrix} = \begin{bmatrix}0.0826 & 0 & 0 \\
0 & 0.0826 & 0 \\
0 & 0 & 0.065
\end{bmatrix}
\begin{bmatrix}v \\ \dot{v} \end{bmatrix} = \tau\]  \(\text{(9)}\)

The transfer function of the turn bow motion is:

\[0.1476\dot{r} + 1.01 \times 10^{-4} r = \tau,\]  \(\text{(10)}\)

C. Identification of water-jet thruster

In order to identify the dynamic characteristics of water-jet thruster. According to the lever principle, a method of measuring the relationship between the input voltage and the output force of the water-jet thruster could be established. As shown in Fig.3 and Fig.4, the experimental device consisted of the angle ruler and fixed mechanism.

Using the lever principle, the relationship between the input voltage and output force can be expressed as the following equation:

\[F_i = mg \cdot \sin\psi\]  \(\text{(11)}\)

where \(\psi\) is the deflection angle of lever, \(m\) is the quality of underwater spherical robot, \(g\) is the gravity.

The experimental data were fitted into a curve by using the MATLAB Curve Fitting Toolbox. Then the relationship between input voltage and deflection angle of the water-jet thruster is shown in Fig.5. The relation curve of input voltage and output force of spray motor is shown in Fig.6.

Second order polynomial curve fitting is adopted for modeling the relationship between input voltage and angle. The equation obtained from the above relationship is:

\[\psi = 0.03545u_i^2 + 0.2382u_i - 0.2369\]  \(\text{(12)}\)

III. TRADITIONAL PID AND FUZZY PID CONTROL METHOD

A. Traditional PID

Traditional PID controller has been widely used in various fields since its appearance, and obtained very good achievements, especially has a vital influence in the industrial production line. It has many advantages, such as simple structure and good stability. The input quantity of PID control is based on the error between the feedback quantity and the desired value, the input quantity is calculated by proportional, integral, differential, and the sum of them is to obtain control quantity.
Generally, traditional PID is suitable for linear systems. Block diagram of traditional PID control system is shown in Fig. 7.

![Fig.7 Block diagram of traditional PID control system]

**PID controller control law is:**

\[
\begin{align*}
\dot{u}(t) &= K_p \left( e(t) + \frac{1}{T_1} \int_0^t e(t) dt + T_d \frac{de(t)}{dt} \right) \\
&= K_p e(t) + K_i \int_0^t e(t) dt + K_d \frac{de(t)}{dt}
\end{align*}
\]  

(14)

where \( K_p \) is proportional gain coefficient, \( K_i \) is integral coefficient, \( K_d \) is differential coefficient, \( e(t) \) is error.

**B. Fuzzy PID**

Fuzzy PID controller consists of two parts: fuzzy module and traditional PID controller. The main task of fuzzy PID controller is to detect the error and the rate of error of the system at each sampling period continuously, and it can obtain the correction quantity of PID parameters according to fuzzy rules. Then, the control quantity of the system is obtained by calculation of the PID controller. Fuzzy PID can improve performance and robustness of system by the tuning of PID parameters at real-time, and increase the anti-interference of the system. Block diagram of the fuzzy PID controller system is shown in Fig. 8.

![Fig.8 Block diagram of fuzzy PID controller system]

The design of fuzzy PID controller can be divided into three step as follows:

1) First step, the fuzzy of input and output variables:

We select the robot’s yawing angle error \( \epsilon(t) \) and its rate of change \( ec(t) \) as the input variables of the fuzzy PID controller. After the input variables are calculated by the quantization factor, we enter them to the fuzzy controller and get the blurring variable \( E \) and \( Ec \). The output of fuzzy variables are \( K_p \), \( K_i \) and \( K_d \). The fuzzy domain and membership functions of input and output variables are shown in Fig. 9 (a) to Fig. 9 (e).

2) Second step, the design of fuzzy rules:

Generally in different cases, the principle of setting of PID parameters as follows:

1) When the value of \(|E|\) is big, we need to increase the value of \( K_p \) so that the \(|E|\) can decrease quickly, and we need to decrease the value of \( K_d \) that can void the fast increase of differential action.

2) When the value of \(|E|\) and the \(|Ec|\) are medium, we need to decrease the value of \( K_p \) and \( K_i \) that can avoid the overshoot.

3) When the value of \(|E|\) is small, we need to increase the value of \( K_p \) and \( K_i \) that can decrease the steady-state error. To avoid instability in the vicinity of the steady-state value of the system, and the dynamic performance of the system will be greatly affected by the value of \( K_d \), so we need to find a suitable value of \( K_d \).

4) The error rate of change of system is decided by the value of \(|Ec|\), and when the value of \(|Ec|\) is big, we need to increase the value of \( K_p \) and decrease the value of \( K_i \).

According to the above, the dynamic performance of system can be influenced by PID parameters, based on a large number of experimental data, we can obtain the excellent response performance of the system by setting the principle of fuzzy PID control parameters rules, and the fuzzy rules of \( K_p \) have shown in Table II. Fuzzy rules of the other parameters can be analogy.

![Fig.9 The membership functions of variables]

**TABLE II FUZZY RULES OF \( K_p \)**

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(3) Third step, fuzzy inference and defuzzification:

According to the fuzzy rules, the fuzzy value output of $K_p$, $K_i$ and $K_d$ are obtained by fuzzy inference and defuzzification. The membership degree of the first fuzzy rule corresponding to $K_p$ is:

$$m_{kp1} = \min\{m_{NB}(E), m_{NB}(EC)\}$$  \hspace{1cm} (15)

The rest can be done in the same manner, we can obtain the membership degree of all fuzzy rules are corresponded to the output of $K_p$ at different error and error rate of change. According to fuzzy rules, the fuzzy value of output of $K_p$ can be defuzzification by using the weighted average method:

$$\Delta K_p = \frac{\sum m_{kp} K_{pj}}{\sum m_{kpj}}$$  \hspace{1cm} (16)

where $K_{pj}$ is the real number of domain of $K_p$.

Similarly, we can obtain the fuzzy output value of $K_i$ and $K_d$ in each sampling period. But these values are still fuzzy values, we need to multiply these values by the scale factor so that we can obtain the actual control output value of $K_p$, $K_i$ and $K_d$, and the PID controller parameters can be updated. The adjustment algorithm is:

$$K_p = K_{p0} + D \ast \Delta K_p$$
$$K_i = K_{i0} + D \ast \Delta K_i$$
$$K_d = K_{d0} + D \ast \Delta K_d$$  \hspace{1cm} (17)

where $D$ is the scale factor.

IV. EXPERIMENTS AND RESULTS

In this section, we carried out some experiments to demonstrate that the fuzzy PID is more suitable to our underwater spherical robot.

Fig.10 shows a video sequence of the forward motion and the totally horizontal forward motion spent about twenty-five seconds. In Fig.10, there were two rulers about two meter in the vertical direction of the pool and a ruler about two point five meter in the horizontal direction of the pool. We carried out several underwater experiments based on traditional PID and fuzzy PID. Each experiment was carried out about ten times. For traditional PID and fuzzy PID, the yawing angle is the amount of feedback of controller. Our underwater spherical robots were programmed to finish forward motion and turn bow motion. The yawing angle can be obtained by using the IMU sensor. Fig.11 shows the relationship between the yawing angle and the time of the robot in the forward motion. Fig.12 shows the relationship between the yawing angle and the time of the robot in the turn bow motion. Fig.13 shows the detail about the change of $K_p$, $K_i$ and $K_d$ when underwater spherical robot turn bow.

As shown in the Fig.11, though the change of yawing angle had not very big based on traditional PID, the maximum error of fuzzy PID was about 0.5 degrees and traditional PID was 1.9 degrees, therefore, we can see that Fuzzy PID have better tracking in the small value of error. As shown in the
Fig.12, we can see that the peak value of yawing angle for fuzzy PID was small than traditional PID, and fuzzy PID have better response velocity, less overshoot and less steady-state error. Therefore, compared with traditional PID, fuzzy PID control method have better dynamic performance. Fig.13 shows the value of $K_p$, $K$, and $K_d$ are reliable by using fuzzy rules.

V. CONCLUSIONS AND FUTURE WORK

The main research of this paper is to achieve the fuzzy PID control method for the underwater spherical robot based on horizontal plane. Firstly, some kinematics analysis of the underwater spherical robot were carried out, and the kinematic equations were obtained, which provided a model reference for the actual experiments. Secondly, the relationship between the thrust of the motor under different voltage was obtained by measuring the thrust of the water-jet thruster, and an output reference was provided for the actual experiments. Thirdly, we carried out some actual experiments to demonstrate the effectiveness of fuzzy PID for underwater spherical robot, and experimental results showed that fuzzy PID for the underwater spherical robot had good robustness and good dynamic performance. With the deepening of research, 3D-based motion control gives us the next experimental goal.

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REFERENCES


