



Tracking Control in Presence of Obstacles and Uncertainties for Bioinspired Spherical Underwater Robots

Chunying Li¹ · Shuxiang Guo^{1,2,3} · Jian Guo³

Received: 17 May 2022 / Revised: 18 August 2022 / Accepted: 22 August 2022
© Jilin University 2022

Abstract

During marine missions, AUVs are susceptible to external disturbances, such as obstacles, ocean currents, etc., which can easily cause mission failure or disconnection. In this paper, considering the strong nonlinearities, external disturbances and obstacles, the kinematic and dynamic model of bioinspired Spherical Underwater Robot (SUR) was described. Subsequently, the waypoints-based trajectory tracking with obstacles and uncertainties was proposed for SUR to guarantee its safety and stability. Next, the Lyapunov theory was adopted to verify the stability and the Slide Mode Control (SMC) method is used to verify the robustness of the control system. In addition, a series of simulations were conducted to evaluate the effectiveness of proposed control strategy. Some tests, including path-following, static and moving obstacle avoidance were performed which verified the feasibility, robustness and effectiveness of the designed control scheme. Finally, a series of experiments in real environment were performed to verify the performance of the control strategy. The simulation and experimental results of the study supplied clues to the improvement of the path following capability and multi-obstacle avoidance of AUVs.

Keywords Path following · Obstacle avoidance · Bioinspired · Spherical underwater robot (SUR) · Lyapunov theory

1 Introduction

Nowadays, AUVs are widely used to perform various tasks, such as exploration, inspection, operations, military research and marine environment's observations [1, 2]. In ocean applications, path planning is an essential tool to complete the specific tasks [3, 4]. However, few studies have addressed the path following control in presence of obstacles, especially, in three-dimensional (3D) space. Thus, a

path following strategy with the capability of obstacle avoidance is urgently need, which improve the accuracy and safety of AUVs.

In recent years, many path following techniques have been studied to satisfy the requirements of complex dynamic environments. Common navigation methods including the Artificial Potential Field (APF) [5], Backstepping Slide Mode Control (BSMC) [6], Fuzzy-based Control (FC) [7], Neural Network (NN), LOS guidance and Map Construction (MC) method [8] are used to solve the path following problem. However, those methods cannot counterweight various requirements, and suitable for different model control strategies. Lalish et al. [9], proposed an algorithm to solve the n-vehicle collision avoidance problem. The controller can guarantee all vehicles to follow the desired path. For robots with different motion modes, due to the differences in the dynamic models, it is necessary to comprehensively consider the robot model, including kinematic and dynamic model. Shen et al. in [10, 11], proposed a novel Lyapunov-based model predictive control in horizontal plane to solve the trajectory tracking problem of AUV. Khalaji et al. [12] have developed a highly nonlinear controller for AUVs based on Lyapunov theory. Some analytic simulation scenarios are carried out to verify the effectiveness of the designed

✉ Shuxiang Guo
guo.shuxiang@kagawa-u.ac.jp

✉ Jian Guo
jianguo@tjut.edu.cn

¹ Graduate School of Engineering, Kagawa University, Takamatsu, Kagawa 761-0396, Japan

² Key Laboratory of Convergence Medical Engineering System and Healthcare Technology, the Ministry of Industry and Information Technology, School of Life Science and Technology, Beijing Institute of Technology, Beijing 100081, China

³ Tianjin Key Laboratory for Control Theory and Applications in Complicated Systems and Intelligent Robot Laboratory, Tianjin University of Technology, Binshui Xidao Extension 391, Tianjin 300384, China

controller. However, this method is challenging to apply in real environments. Liu et al. [13] proposed a guidance law to track the reference path safely in vertical plane using the barrier Lyapunov function. However, the above studies are all based on the analysis of simplified models, mostly solves problems in the planner, which cannot meet the needs of multiple underwater missions and extend to the spatial trajectory tracking control.

Moreover, there also exist other methods, such as Model Predictive Control (MPC) [10, 14], Dynamic Window Approach (DWA) [15] and Adaptive Control (AC), to solve the trajectory tracking problem [16, 17]. Zhang et al. [18] proposed the adaptive NN control for robotic manipulators to handle the unmodeled and uncertain dynamics. The NN is applied to achieve full-state feedback for robots. Yan et al. [19] designed a controller for AUV combining with Particle Swarm Optimization (PSO) and Waypoint Guidance (WG). However, the chattering phenomenon and smooth transition has not been solved in the above papers. Although above studies have developed new tools and solutions for 3D path following, they often have low accuracy for avoiding moving obstacles and make them restricted to apply in practice.

In our previous research, a SUR is developed which inspired by the propulsion mechanism of jellyfish [20–22]. The natural jellyfish are mainly composed of a round umbrella, tentacles, mouth and wrist, etc., which spray water in the body by compressing and deforming the body's umbrella membrane to generates propulsion. By spraying water, areas with different pressure levels will be created around the body, and then jellyfish swims in the opposite directions. To imitate the advantages of jellyfish locomotion in symmetry, stability and performance, the SUR's locomotion mechanism uses a hybrid propulsion system composing by a propeller and a water-jet thruster. The proposed hybrid propulsion system provided alternative methods for approaching targets stably, quickly and effectively. The hydrodynamic parameters, such the viscous coefficient, the drag coefficient and the pressure contour of motions we analyzed in [23, 24]. In our previous controllers, [2, 7, 25] there is still instability in trajectory tracking due to the lack of consideration of the correctness of robot modeling and the complexity of the operating environment. Thus, to design the nonlinear control law for SUR safely and accurately, and improve the robot stability, the real-time obstacle avoidance considering SUR modeling is integrated to the trajectory tracking.

As can be seen from the mentioned literature, most controllers neglect terms, such as robustness, stability and the capability of obstacle avoidance in 3D environment. In addition, the parameters, such as size (radius), uncertainties, internal and external disturbances are ignored, which lead to the instability of the whole system. Therefore, considering the complexities, nonlinearities and uncertainties

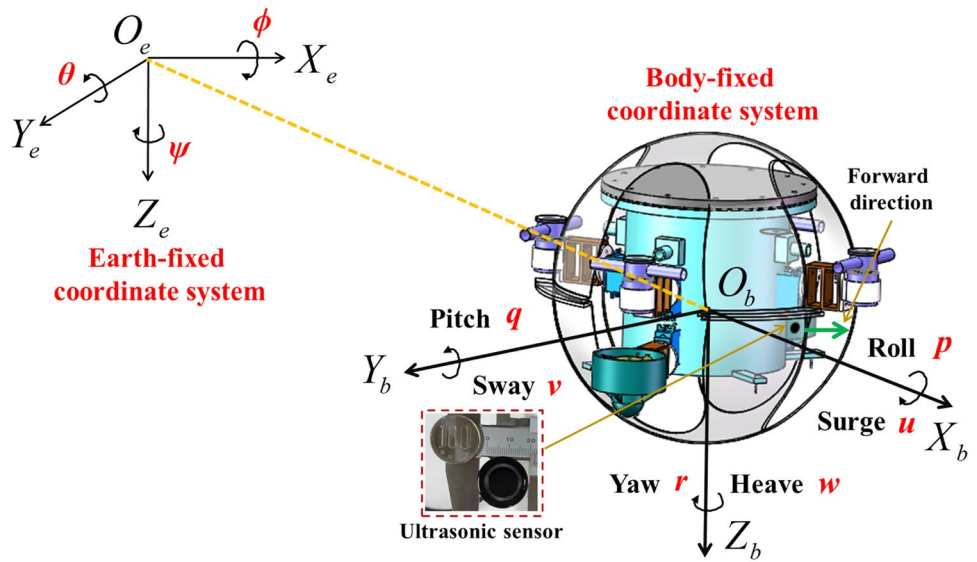
of the AUV's model in ocean environment, in this study, to follow the reference path in real-time and avoid obstacles accurately, a novel control strategy for SUR is employed.

Motivated by the above consideration, this study concentrates on the path following and obstacle avoidance (the static and moving obstacle) for SUR in 3D environment. Compared with our previous control methods, considering the stability and uncertainty of the control system, the kinematic and dynamic model of SUR are established and analyzed. A novel control strategy is developed for SUR, including path following, static and moving obstacle avoidance. Under the principle, the SUR can move and avoid obstacles along the reference trajectory. Moreover, The Lyapunov theory and SMC method are developed and implemented for SUR based on the control strategy to compensate for errors in model uncertainties and external disturbances. Furthermore, the APF method is employed into the proposed control system, which is more suitable for local real-time obstacle avoidance. Besides, the robustness, efficiency of the novel control strategy is examined and validated via a series of simulation and experiments in real environment.

The remainder of this paper is organized as follows: first, we describe the kinematic and dynamic model of SUR, and the path-following and obstacle avoidance is proposed in Sect. 2. Then, the control strategy for SUR is developed, and the stability and robustness of the proposed strategy is verified using Lyapunov and SMC method in Sect. 3. Next, Sect. 4 uses the simulation to display the performance of the proposed strategy, the SUR model established and imported to Webots, a series of experiments are carried out. Then, Sect. 5 uses the SUR to perform a series of experiments in real environment, the tracking trajectories are analyzed. In addition, Sect. 6 discusses the results of some simulation and experiments in real environment. Finally, Sect. 7 presents our conclusions.

2 Kinematic and Dynamic Model of the SUR

The structure of SUR is highly symmetrical, and the four water-jets and two propellers are located above and below the central track, respectively. The forward direction of SUR is perpendicular to the plane, where the propellers and water-jets are located. As shown in Fig. 1, the general kinematic and dynamic models of AUVs [26–28] can be described using the earth-fixed coordinate system (O_e, X_e, Y_e, Z_e) and the body-fixed coordinate system $\hat{u}$. Among them, the ultrasonic sensor is located under the central track and is fixed on the robot body through a bracket to make it consistent with the forward direction of the SUR. In this study, the 6-DOF nonlinear kinematic motion of SUR can be expressed as follows:

Fig. 1 Coordinate frames of the SUR

$$\dot{\eta} = J\Theta(\eta)v$$

$$(1) \quad M\dot{v} + C(v)v + D(v)v + g(\eta) = \tau + \omega_e \quad (3)$$

where $\eta = [x, y, z, \phi, \theta, \psi]^T$ is the state vector which included the position $[x, y, z]$ and orientation $[\phi, \theta, \psi]$ in the earth-fixed frame, $v = [u, v, w, p, q, r]^T$ is the vector which included the linear velocity $[u, v, w]$ and angular velocity $[p, q, r]$. $J_\Theta(\eta)$ is the transformation matrix between the earth-fixed and robot's body-fixed frame, it is formalized as

$$J_\Theta = \begin{bmatrix} c\psi c\theta & c\psi s\theta s\phi - s\psi c\phi & c\phi s\theta c\psi + s\psi s\phi & 0 & 0 & 0 \\ s\psi c\theta & s\psi s\theta s\phi + c\psi c\phi & c\phi s\theta s\psi - c\psi s\phi & 0 & 0 & 0 \\ -s\theta & s\phi c\theta & c\phi c\theta & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & s\phi t\theta & c\phi t\theta \\ 0 & 0 & 0 & 0 & c\phi & -s\phi \\ 0 & 0 & 0 & 0 & s\phi/c\theta & c\phi/c\theta \end{bmatrix} \quad (2)$$

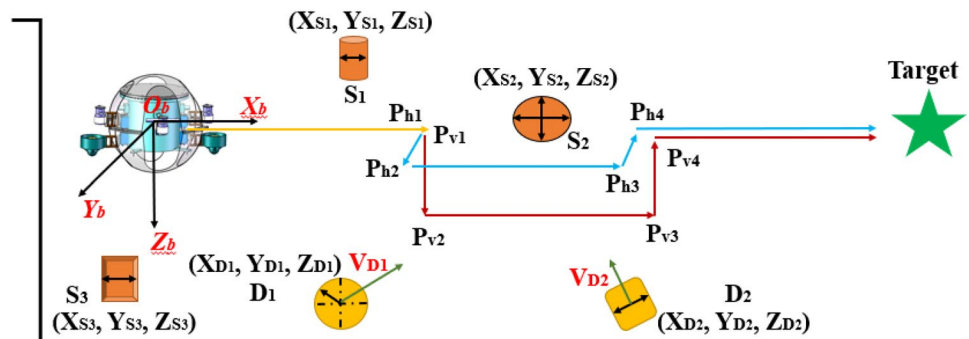
where s , c and t are the abbreviations of sin, cos and tan, respectively.

The dynamic model of the SUR can be expressed as follows:

where $M \in R^{6 \times 6}$ is the inertia matrix, $C(v) \in R^{6 \times 6}$ represents the Coriolis-centripetal matrix, $D(v) \in R^{6 \times 6}$ describes the hydrodynamic damping matrix, $g(\eta) \in R^{6 \times 1}$ expresses the restoring forces and moments (gravity and buoyancy), $\tau \in R^{6 \times 1}$ describes the forces and moments acting on the SUR, $\omega_e \in R^{6 \times 1}$ is the vector of the time-varying external disturbances.

Because the SUR is an underactuated system, it mainly realizes underwater obstacle avoidance and positioning through horizontal or vertical motion during performing tasks, as shown in Fig. 2. Among them, S (S_1, S_2, S_3) and D (D_1, D_2) represent the static obstacle and moving obstacle, respectively. Therefore, to facilitate later controller design, the horizontal and vertical motion equations are decomposed.

The mathematical model of the horizontal and vertical plane for SUR can be rewritten as

Fig. 2 Schematic diagram of the SUR when performing underwater missions

$$\begin{cases} \dot{x} = u \cos \psi - v \sin \psi \\ \dot{y} = u \sin \psi + v \cos \psi \\ \dot{\psi} = r \end{cases} \quad (4)$$

$$\begin{cases} \dot{x} = u \cos \theta - v \sin \theta \\ \dot{z} = u \sin \theta + v \cos \theta \\ \dot{\theta} = q \end{cases} \quad (5)$$

where (x, y) , and (x, z) are the horizontal and vertical vector of the SUR, respectively.

Using the Lagrange method to extract the SUR dynamic model, the results satisfy:

$$\begin{cases} \dot{u} = \frac{m_{22}}{m_{11}}vr - \frac{X_u}{m_{11}}u - \frac{X_{u|u}|u| + F_u}{m_{11}} \\ \dot{v} = -\frac{m_{11}}{m_{22}}ur - \frac{X_v}{m_{22}}v - \frac{Y_{v|v}|v| + F_v}{m_{22}} \\ \dot{r} = \frac{m_{11} - m_{22}}{m_{33}}uv - \frac{N_r}{m_{33}}r - \frac{N_{r|r}|r| + g_r}{m_{33}} \end{cases} \quad (6)$$

$$\begin{cases} \dot{u} = -\frac{m_{44}}{m_{11}}uw - \frac{X_u}{m_{11}}u - \frac{X_{u|u}|u| + F_u}{m_{11}} \\ \dot{w} = \frac{m_{11}}{m_{55}}uw - \frac{Z_w}{m_{55}}w - \frac{Z_{w|w}|w| + F_w}{m_{55}} \\ \dot{q} = \frac{m_{11} - m_{44}}{m_{66}}uw - \frac{M_q}{m_{66}}q - \frac{M_{q|q}|q| + g_q}{m_{66}} \end{cases} \quad (7)$$

where F_u, F_v, F_w are the lateral and longitudinal forces, respectively; $m_{11}, m_{22}, m_{44}, m_{55}$ are the parameters of added mass, m_{33} and m_{66} represents the added moment; And $X_u, Y_v, Z_w, N_r, M_q, X_{u|u}, Y_{v|v}, Z_{w|w}, N_{r|r}, M_{q|q}$ is the drag coefficient, respectively, g_r, g_q are the uncertain terms.

2.1 Implemented Trajectory Tracking

To facilitate later controller design for SUR, considering the kinematic control and obstacle avoidance, the following guidance law is proposed:

$$\begin{cases} \dot{x} = u \cos \psi \\ \dot{y} = -u \sin \psi \\ \dot{\psi} = r \end{cases} \quad (8)$$

$$\begin{cases} \dot{x} = u \cos \theta \\ \dot{z} = -u \sin \theta \\ \dot{\theta} = q \end{cases} \quad (9)$$

where r, q represent the angle between SUR and the horizontal or vertical planes, which guide the robot converge to the

adjacent waypoint. In addition, ψ, θ is bounded and converge to the SUR's horizontal and vertical plane model.

To make SUR follow the reference path, the guidance strategy is proposed, which is very necessary to complete tasks. The starting point and the target point are defined as $(X_{sp}, Y_{sp}), (X_{tp}, Y_{tp})$, respectively. The waypoints (X_i, Y_i) are established to following the reference path, as shown in Fig. 3.

The 3-D trajectory tracking problems of SUR can often use the following equation to define the tracking errors (see [3, 18, 29–31], for example):

$$\begin{bmatrix} x_e \\ y_e \\ \psi_e \end{bmatrix} = \begin{bmatrix} c\psi c\theta & s\psi c\theta & -s\theta \\ -s\psi & c\psi & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x - x_d \\ y - y_d \\ \psi - \psi_d \end{bmatrix} \quad (10)$$

$$\begin{bmatrix} x_e \\ z_e \\ \theta_e \end{bmatrix} = \begin{bmatrix} c\psi c\theta & s\psi c\theta & -s\theta \\ s\theta c\psi & s\theta s\psi & c\theta \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x - x_d \\ z - z_d \\ \theta - \theta_d \end{bmatrix} \quad (11)$$

It can be seen that the trajectory tracking error of SUR's dynamic model is coupled and complex. In this paper, the tracking error is defined as $\mathbf{e} = \boldsymbol{\eta} - \boldsymbol{\eta}_e$ to maneuver the SUR for precisely tracking the trajectory and guarantee the safety of SUR during obstacle avoidance. Among them, $\boldsymbol{\eta}_e = [x_e, y_e, \psi_e]^T$ or $\boldsymbol{\eta}_e = [x_e, z_e, \theta_e]^T$ represents the desired position trajectory.

2.2 Implemented Obstacle Avoidance Mode

Considering the obstacle avoidance is necessary for path following of AUVs [32–36], to provide the ability of rounding of obstacles, an obstacle avoidance mode is developed and added to the main following controller.

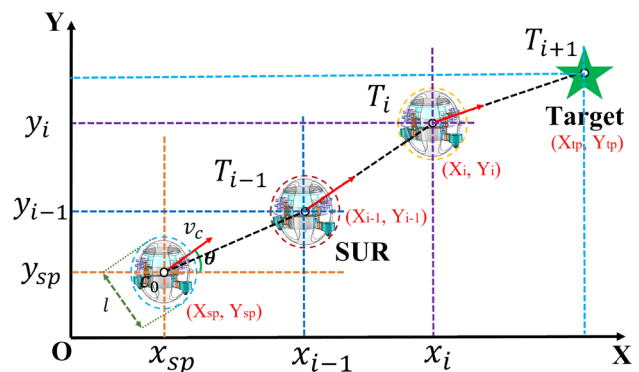


Fig. 3 Framework of the path following for spherical underwater robot

As the eyes of AUVs, sensors are an indispensable tool for sensing the ocean and the surrounding environment, especially the application of underwater obstacle avoidance. Compared with other sensor detection methods, ultrasonic sensor system is widely used because of its low-cost, easy-installation, and not easy to be disturbed by electromagnetic and light. Thus, in this paper, the underwater ultrasonic module (JSN-SR04) is used to improve the obstacle avoidance capability of SUR and complete the mission. The relationship between ultrasonic sensor and SUR is shown in Fig. 1. The detection angle is less than 50° and the resolution is about 5 mm. In the simulation, in Sect. 4, the trajectory tracking and obstacle avoidance performance tests are performed by adding sensor nodes in Webots. Ultrasonic sensor parameters are set with reference to parameters of JSN-SR04. In addition, we also use the ultrasonic module to perform a series of obstacle avoidance experiments in Sect. 5 to verify the effectiveness of the proposed control strategy.

The moving obstacle satisfy the equation:

$$\begin{cases} \dot{x}_{MO} = u_{MO} \cos \theta_{OB} \\ \dot{z}_{MO} = -u_{MO} \sin \theta_{OB} \end{cases} \quad (12)$$

where x_{MO} and z_{MO} represent the position, and θ_{MO} is the attitude of moving obstacle, u_{MO} represents the velocity. The position relationship between the robot and obstacle satisfies:

$$D = \sqrt{(x_O - x_b)^2 + (z_O - z_b)^2} \geq D_t \quad (13)$$

where D_t represents the distance between the SUR and the obstacle at time t .

In underwater environment, the SUR may encounter the static (Fig. 4a) and moving obstacles (Fig. 5b), as shown in Fig. 4. Considering the possibility of tracking control for SUR, the static obstacle and moving obstacle is analyzed to track reference path safely [8]. When SUR detects the static obstacle, as shown in Fig. 4a, if the condition $D < R_s, \theta_d < \beta$ is satisfied, the static obstacle avoidance is activated. D is the shortest distance between the SUR and the obstacle center, β is the angle between the tangent which pass the center of gravity of SUR and horizontal line. Noted that the static obstacle avoidance is a special

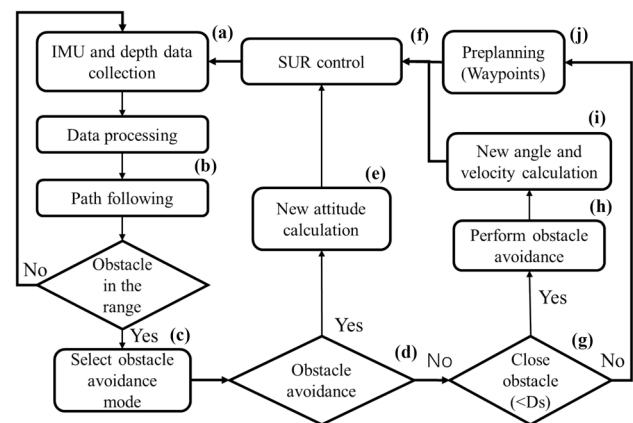


Fig. 5 The path-following strategy for SUR in presence of obstacles, among them, detecting obstacles (a–c), and performing obstacle avoidance behavior (others)

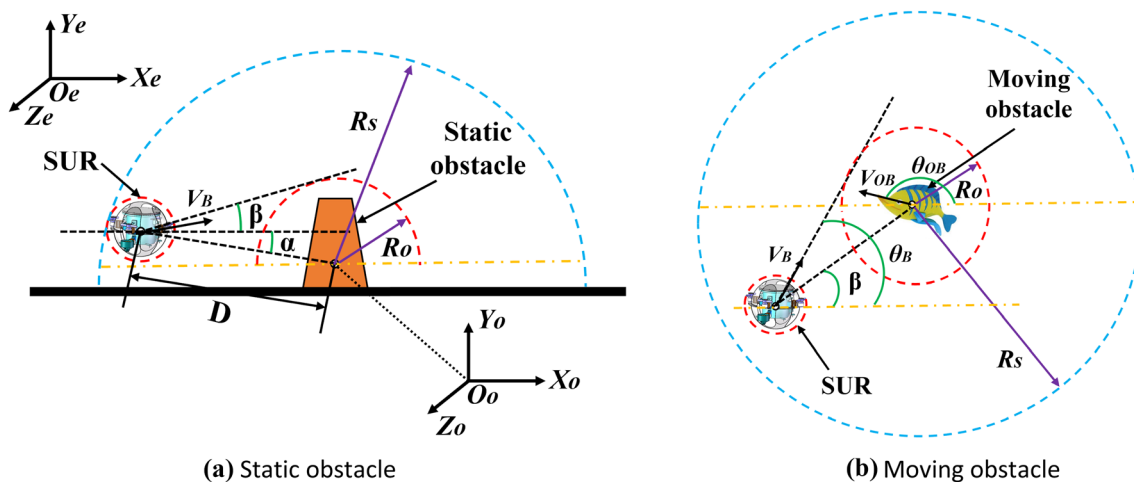


Fig. 4 Principle and related parameters for SUR's obstacle avoidance. **a** The principle of obstacle avoidance under the static obstacle; **b** The principle of obstacle avoidance under the moving obstacle

case of moving obstacle avoidance, which will be further verified in Sect. 3.

3 Control System for SUR

3.1 Tracking Mode

Considering the coupling, nonlinearity and complexity of the SUR model, the simplified tracking error model is proposed in this section:

$$\begin{cases} x_e = (x - x_d) \cos \beta + (y - y_d) \sin \beta \\ y_e = -(x - x_d) \sin \beta + (y - y_d) \cos \beta \\ z_e = z - z_d \end{cases} \quad (14)$$

After the above analysis, the Lyapunov function is used to prove the stability of SUR:

$$V_1 = \frac{1}{2} e_t^2 = \frac{1}{2} (x_e^2 + y_e^2) \quad (15)$$

The time derivation of V_1 yields:

$$\dot{V}_1 = e_t \dot{e}_t = x_e (u \cos \beta - u_d \cos \beta_d) + y_e (u \sin \beta - u_d \sin \beta_d) \quad (16)$$

where $x_e = l \cos \beta$, $y_e = l \sin \beta$, l is the distance between current position and next position, and β_d is the virtual angle that is dynamically assigned to follow SUR and avoid obstacles.

Then, we can obtain:

$$\begin{aligned} \dot{V}_1 &= l(-u_d(\cos^2 \beta_d + \sin^2 \beta_d) + \cos(\beta - \beta_d)) \\ &= -k_1 l^2 \leq 0 \end{aligned} \quad (17)$$

where k_1 is a positive constant.

3.2 SMC Method for SUR's Dynamic

Then, we used the SMC method to ensure the robustness of the system in disturbances based on Lyapunov function. The design procedures are as follows:

Step 1: The error variables z_1 and z_2 are defined as follows:

$$z_1 = \psi - \psi_d \quad (18)$$

$$\dot{z}_1 = \dot{\psi} - \dot{\psi}_d = r - \dot{\psi}_d \quad (19)$$

$$z_2 = \dot{z}_1 + k_2 z_1 \quad (20)$$

where $k_2 > 0$ is a feedback gain, and z_1 is the angle error. Then, the first Lyapunov function V_2 is defined as

$$V_2 = \frac{1}{2} z_1^2 \quad (21)$$

$$\dot{V}_2 = z_1 \dot{z}_1 = z_1(r - \dot{\psi}_d) = z_1(z_2 - k_2 z_1) = z_1 z_2 - k_2 z_1^2 \quad (22)$$

The switching function for sliding mode is expressed as S_{11} :

$$S_{11} = k_3 z_1 + z_2 = (k_2 + k_3) z_1 + \dot{z}_1 \quad (23)$$

where $k_3 > 0$. It is obvious that $z_1, z_2 = 0$ if $S_{11} = 0$, then $\dot{V}_2 \leq 0$.

Step 2: The second Lyapunov function is expressed using S_{11} as follows:

$$V_3 = V_2 + \frac{1}{2} S_{11}^2 \quad (24)$$

$$\dot{V}_3 = \dot{V}_2 + S_{11} \dot{S}_{11} = -k_2 z_1^2 + z_1 z_2 + S_{11} [k_3(z_2 - k_2 z_1) + \ddot{\psi} - \ddot{\psi}_d + k_2 \dot{z}_1] \quad (25)$$

Then, the control law is expressed as follows:

$$f_r = -k_3(z_2 - k_2 z_1) - \ddot{\psi} + \ddot{\psi}_d - k_2 \dot{z}_1 - h_1(S_{11} + \varepsilon_1 \operatorname{sgn}(S_{11})) \quad (26)$$

where $h_1, \varepsilon_1 > 0$, Substituting (25) into (24) yields:

$$\dot{V}_3 = -k_2 z_1^2 + z_1 z_2 - h_1 S_{11}^2 - h_1 \varepsilon_1 |S_{11}| \quad (27)$$

To deal with $\dot{V}_3$, a symmetric matrix Q is defined as follows:

$$Q = \begin{bmatrix} k_2 + h_1 c_1^2 & h_1 c_1 - \frac{1}{2} \\ h_1 c_1 - \frac{1}{2} & h_1 \end{bmatrix} \quad (28)$$

Therefore, $\dot{V}_3$ can be rewritten as

$$\dot{V}_3 \leq -z^T Q z - h_1 \varepsilon_1 |S_{11}| \quad (29)$$

According to the asymptotic stability theorem, if the partial derivative V_3 satisfies that $\dot{V}_3$ is negative definite or semi-negative definite, then the control system is asymptotically stable. Therefore, we can obtain that (28) satisfies that $\dot{V}_3 \leq 0$ if Q is positive definite matrix, and the control system is asymptotically stable under the following condition:

$$\begin{aligned} |Q| &= h_1(k_2 + h_1 c_1^2) - \left(h_1 c_1 - \frac{1}{2}\right)^2 \\ &= h_1(k_2 + c_1) - \frac{1}{4} \end{aligned} \quad (30)$$

3.3 Obstacle Avoidance Capability

Based on the above obstacle avoidance analysis in Sect. 2, we also use the Lyapunov function candidate to verify that the SUR can converge to the boundary of the anti-obstacle area $R_o \leq R \leq R_s$:

$$V_4 = \frac{1}{2} e^2 \quad (31)$$

The time derivation along V_4 is

$$\dot{V}_4 = e\dot{e} = e(\dot{D} - \dot{R}_o) \quad (32)$$

Based on the definition β (in Fig. 4b), the relationship between D and β can be rewritten as

$$\begin{cases} D \cos \beta = x_{MO} - x_d \\ -D \sin \beta = z_{MO} - z_d \end{cases} \quad (33)$$

Substituting (12), (32) into (31) obtains:

$$\begin{aligned} \dot{V}_4 &= e \frac{D \cos \beta (\dot{x}_O - \dot{x}_d) - D \sin \beta (\dot{z}_O - \dot{z}_d)}{D} \\ &= e[u_{MO} \cos(\beta - \theta_{OB}) - u_d \cos(\theta_d - \beta)] \end{aligned} \quad (34)$$

where $\theta_d = \beta + \pi/2 - \arctan(z_{MO} - z_d)/(x_{MO} - x_d)$. Then, (33) can be written as

$$\begin{aligned} \dot{V}_4 &= e \left[u_{MO} \cos(\beta - \theta_{OB}) - u_{dMO} \cos \left(\frac{\pi}{2} - \arctan \frac{z_{MO} - z_d}{x_{MO} - x_d} \right) \right] \\ &\leq - \frac{u_{dMO} e^2}{\sqrt{(z_{MO} - z_d)^2 + (x_{MO} - x_d)^2}} = - \frac{2u_{dMO}}{\sqrt{(z_{MO} - z_d)^2 + (x_{MO} - x_d)^2}} V_4 \end{aligned} \quad (35)$$

Considering $t \rightarrow \infty$, V_4 approaches 0, thus, the stability is guaranteed.

In this study, the APF method is used to improve the capability of local obstacle avoidance. Compared to numerical methods, this method refrains offline entity and local minimization problems, also enhancing the ability to pass moving obstacles.

The repulsive potential function is considered as

$$P_{rep} = 1 / \left\| \frac{D_{obs}}{R_s} \right\| + \log \left\| \frac{D_{obs}}{R_s} \right\| \quad (36)$$

where $D_{obs} = D$ is the momentary shortest distance between the SUR and the center of obstacle, and R_s is the radius of the surrounded area of obstacles. According to $f_{rep} = -\gamma \nabla P_{rep}$, we have

$$\begin{cases} f_{rep,x} = -\gamma(x - x_o) \frac{(D_{obs}^2 - R_s^2)}{D_{obs}^6} \\ f_{rep,y} = -\gamma(y - y_o) \frac{(D_{obs}^2 - R_s^2)}{D_{obs}^6} \\ f_{rep,z} = -\gamma(z - z_o) \frac{(D_{obs}^2 - R_s^2)}{D_{obs}^6} \end{cases} \quad (37)$$

where γ is an adjustable obstacle avoidance gain. Adding the obstacle avoidance feature f_{rep} , to resist external disturbance, enhance stability and avoid jitter phenomenon, the continuous function $\theta(s)$ is used. Thus, the controlling input of SUR dynamic system can be written as follows:

$$f = M^{-1}(\ddot{\eta} - C_{input} + \Omega \epsilon - K\theta(s) + f_{rep}) \quad (38)$$

where C_{input} is determined by the horizontal dynamic equation, vertical dynamic equation of SUR, and the input vector; Ω and K are the positive definite gain matrix and the diagonal controlling gain, respectively.

According to the above analysis, the effectiveness of the avoidance capability for SUR is verified.

4 Simulation Results

In this section, some simulation scenarios are performed to verify the effectiveness, stability and efficiency of the proposed path-tracking and obstacle avoidance scheme. Compared to the traditional method, the Webots software is adopted to design the scenarios which consider the SUR's model and parameters, such as mass, thrusters and joints, etc. In addition, it simulates the dynamic effects realistically and verify the algorithm performance effectively.

Based on the above controller stability and robustness analysis, we construct a path following strategy, as shown in Fig. 5. The trajectory tracking strategy is implemented by adding related sensors and parameters setting in Webots.

4.1 Simulation Setup

Webots is physics robotics simulation software, which can be used for creating robot prototype or achieving autonomous control. After importing the SUR model, the parameters, such as liquid environment and node of SUR, are set in Table 1. Ultrasonic sensor is configured, including distance, detection angle, etc. Controllers are then specified through Webots Application Programming Interface (API). The sensor is activated using the enable function. In this paper, the

Table 1 Specific features of the SUR prototype in simulation

Parameters	Values
Diameters	540 mm
Total mass	Approx. 7.9 kg
Drive mode	Servo motors and DC motors
Sensors	Ultrasonic module, depth sensor, IMU etc
Density of liquid	1000 kg/m ³ (in the freshwater environment)
Dynamic viscosity coefficient	μ : 1.219×10^{-3} kg m ⁻¹ s ⁻¹ η : 0.899×10^{-6} kpa·s
Gravity	9.81 kg/m ³
Temperature	25 °C
Reference area	xyz-projection

SUR works in 3D environment and follows the reference path in presence of the static and moving obstacles.

After completing the setup of sensors, node properties of robot and underwater environment, we built the corresponding controller using C++. SUR completes obstacle avoidance of moving and static obstacles by following reference path to verify the performance of the proposed control strategy (SMC–APF).

4.2 Simulation Results

4.2.1 Case Study 1

In this part, the capabilities that the SUR follow the reference trajectory is explored. To verify the path following capability of SUR in 3D environment, the reference path is designed as shown in Fig. 6, which is to effectively verify the above path following strategy, in Sect. 3. Noted that, in the underwater environment, we set a certain disturbance acting on the underwater robot to check the robustness of the SMC–APF.

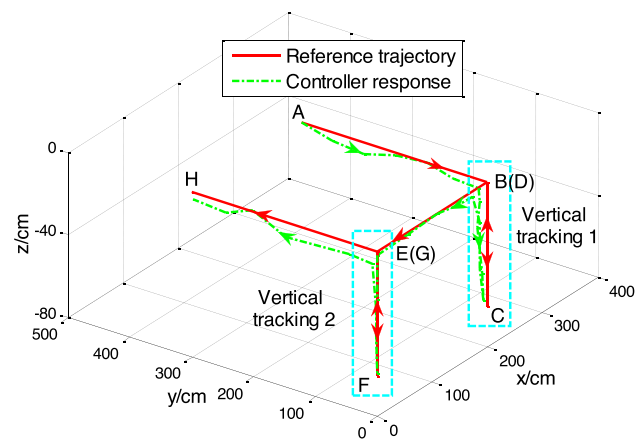
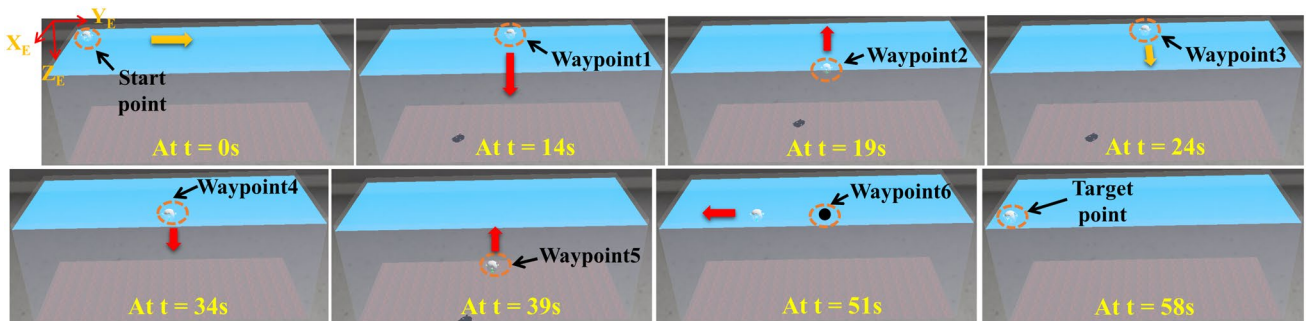
The process of the path-following: first, the SUR starts from the starting point, follows the reference trajectory to the Waypoint1, and then performs the diving locomotion

(Waypoint1) and the ascending motion (Waypoint2), which is to verify the capability of path-following in the vertical plane, from 14 to 24 s. Then, SUR will continue to follow the reference path to the Waypoint4, and perform the path-following in the vertical plane continuously, from the Waypoint4 to the Waypoint6. Finally, SUR will follow the rest of the path, until to the target point.

To show the superiority of the SMC–APF, the trajectory of the SUR for tracking the reference path is obtained, as shown in Fig. 7, which depict the comparison of the desired path and actual trajectory of the SUR. It can be seen that the robot can track the reference path successfully and the trajectory is smooth.

4.2.2 Case Study 2

AUVs need to track the different desired paths, to verify the capability of the SMC–APF to bypass the obstacles, two scenarios are considered, the static obstacle and moving obstacle, in the next section. Based on the above analysis, the SUR is supposed to track the similar trajectory, so in this part, we add three static obstacles to track the trajectory, and

**Fig. 7** Path following results of the SUR in 3D environment**Fig. 6** Path following experiments for SUR in 3D environment

the capability of the obstacle avoidance in different plane is integrated, as shown in Fig. 8.

The process of the static obstacle avoidance: first, the SUR starts from the starting point, and follows the reference trajectory (cruise 1). When the static obstacle (S1) is detected, the obstacle avoidance on the vertical plane will be triggered (obstacle avoidance 1). Note that when the distance detected obstacle on the vertical distance is less than or equal to the distance in horizontal plane, the obstacle avoidance will be triggered prioritized. When the obstacle is bypassed, the SUR will perform the behavior (cruise 2) continually. Then, when the static obstacle (S2) is detected, the obstacle avoidance 2 will be triggered. Using this benchmark until the SUR reaches the target point. Noted that, the obstacle (S3) is specially considered to verify obstacle avoidance in the horizontal plane.

As can be seen from Fig. 9, the SMC-APF passes the obstacles successfully, the actual trajectory is close to the reference trajectory. S1, S2 and S3 indicates the obstacle avoidance area of SUR.

4.2.3 Case Study 3

After the static obstacle avoidance is analyzed, the moving obstacle is added, we use the SUR as the moving obstacle which is operated around the reference path, as shown in Fig. 10.

It can be seen from Fig. 10 that the SUR is performing the moving obstacle avoidance. Before 7 s, the SUR first complete the cruise mission along the reference path. When the moving obstacle is detected, the obstacle avoidance behavior is triggered, and SUR will find a safe path using guidance principle to avoid obstacle. After 17 s, the SUR will follow

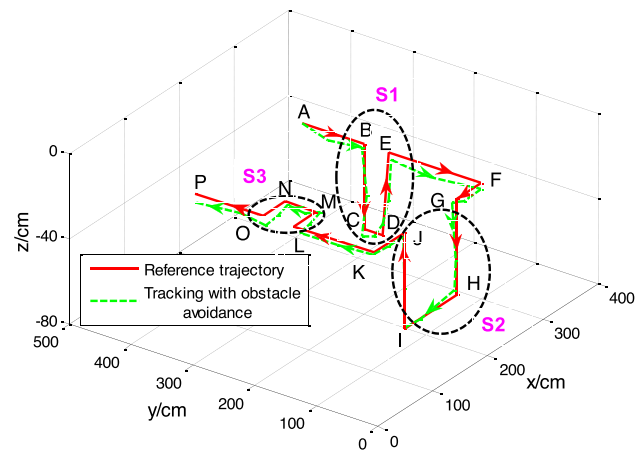


Fig. 9 Path following results in presence of static obstacles

the reference path and avoid obstacle, at the time = 54 s, the SUR reaches the target point.

Figure 11 displays the overall trajectory of the SUR. The trajectory of SUR verifies the capability of guidance law to the static and moving obstacle, we also can see that the SUR can quickly switch to the path-following mode after avoiding obstacle. S2 and S3 indicates the area of the static obstacle, and D1 indicates the area of the moving obstacle.

5 Experimental Results

After some simulation experiments are performed, to further verify the effectiveness of proposed self-guided and obstacle avoidance strategy, some experiments in the real environment are carried out, including tracking and avoiding obstacle experiments. Noted that in the multi-obstacle

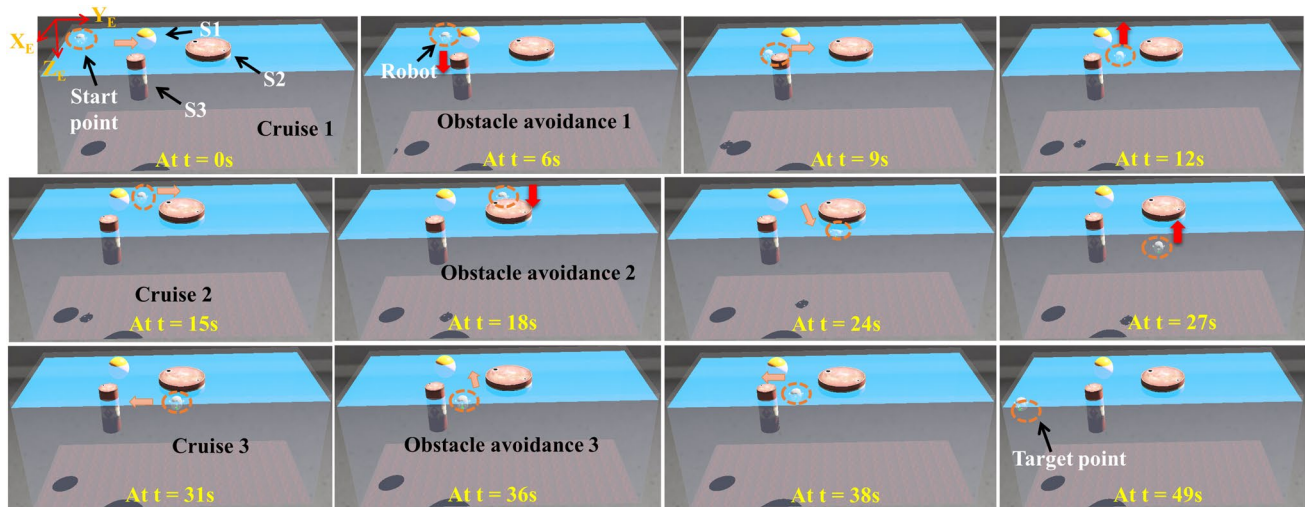


Fig. 8 Path following experiments in presence of static obstacles

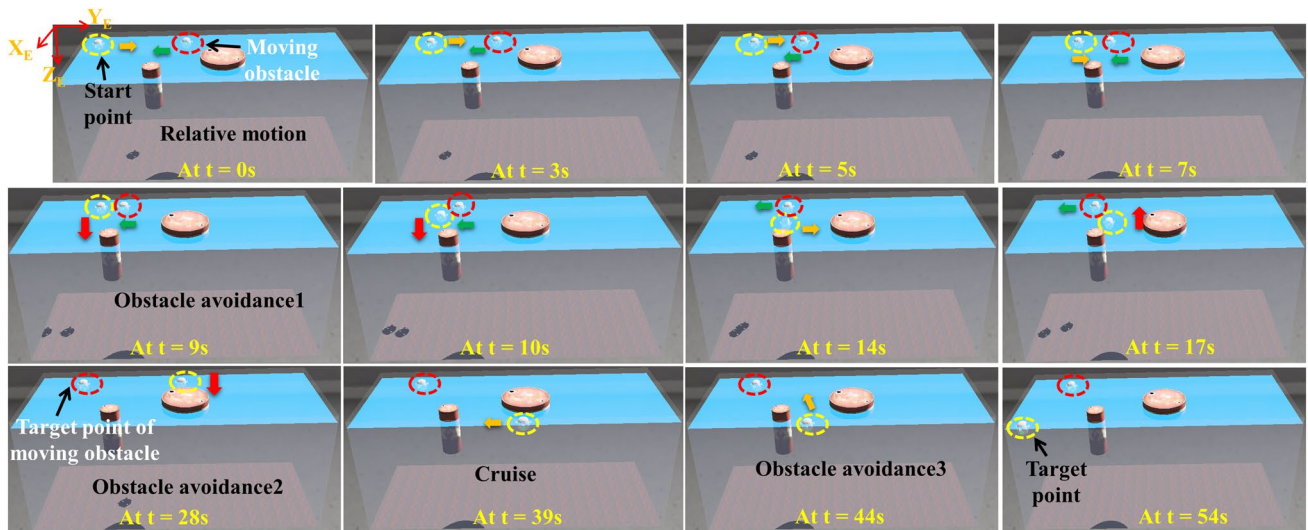


Fig. 10 Path-following experiments with static obstacle and moving obstacle

experiments, only two static obstacles and one moving obstacle are set on the reference path due to limit of the size of the experimental pool.

5.1 Control System Setup

To improve the stability and logic of the control system, four parts, including Power supply layer, Decision layer, Sensor layer and Driving layer, are divided. The power monitoring system consists of three detachable batteries, one (Battery I) is used for powering the Control system and Sensor layer, and two (Battery II) is used for powering the hybrid drive device and steering engine. Battery working time is typically about 2 h during experiments. The Ultrasonic sensor can be used to collect surrounding information to ensure the

robot perform tasks safely. The IMU and pressure sensor is utilized and used to perceive and adjust the robot attitude. The communication device (Micron data modem (Tritech)) is used for real-time communication.

During the tracking process, the current position of the SUR is obtained by processing the data of the IMU 9250 and Depth sensor JY901 to realize the positioning and navigation of the robot. The characteristic of the SUR is described in Table 2. In the Control system, a complementary filtering algorithm is adopted to estimate the data, which is detailed in [3], and the position of the SUR is fed back in real-time to achieve a guided closed-loop. During underwater motion, we also define the Earth-fixed coordinate system and body-fixed coordinate system. The motion state is obtained by calculating the distance between the initial position and the current position of the robot.

5.2 Performance of Tracking Experiments

To verify the effectiveness of the SMC–APF for SUR, first, the tracking experiment is performed, as shown in Fig. 12. The robot starts from the initial position, at time = 0 s (point A). When the robot reaches the point B and C, tracing on the vertical plane will be performed, namely, the diving and ascending process. About time = 34 s, the SUR reaches the target position. Due to some external factors, such as water waves and wind, the markers will move in a small range, which is also one of the reasons for the relatively large error in the real environment. The tracking trajectory of the SUR is shown in Fig. 13. It can be seen that the SUR can track the reference trajectory successfully using the proposed control strategy. Due to the limited depth of the pool, the set depth is 50 cm in this paper.

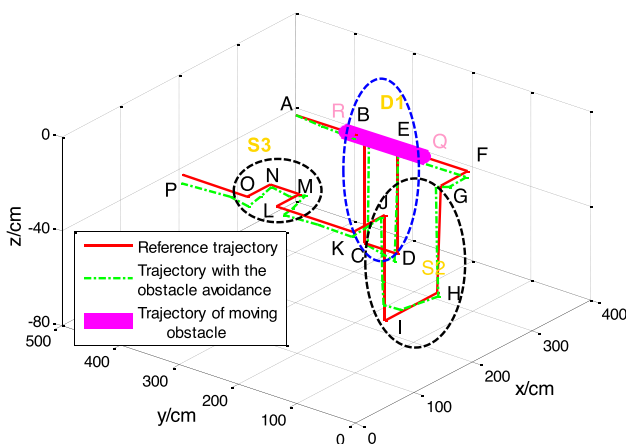
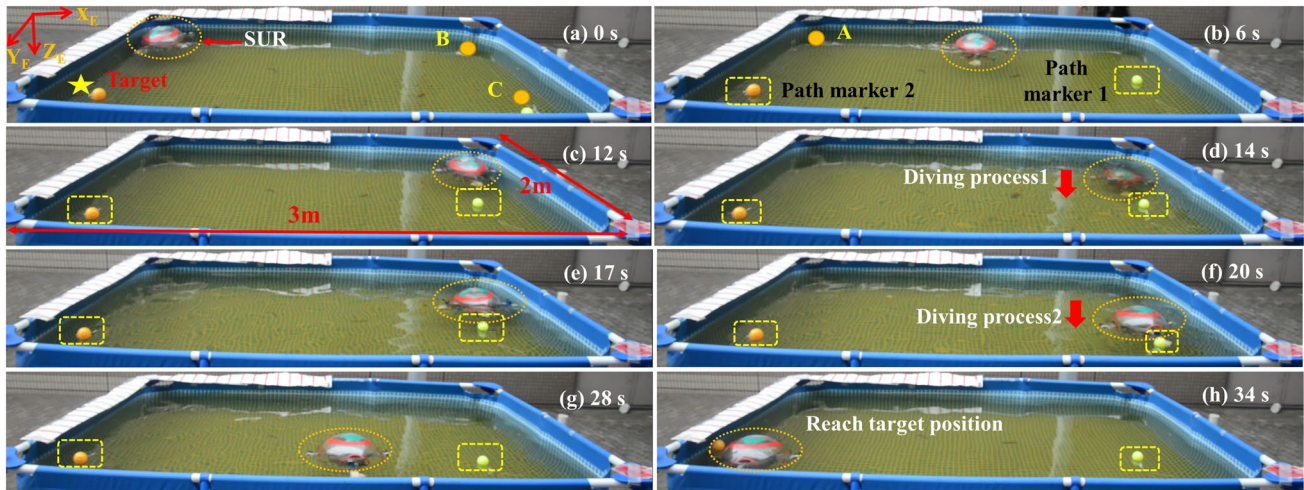
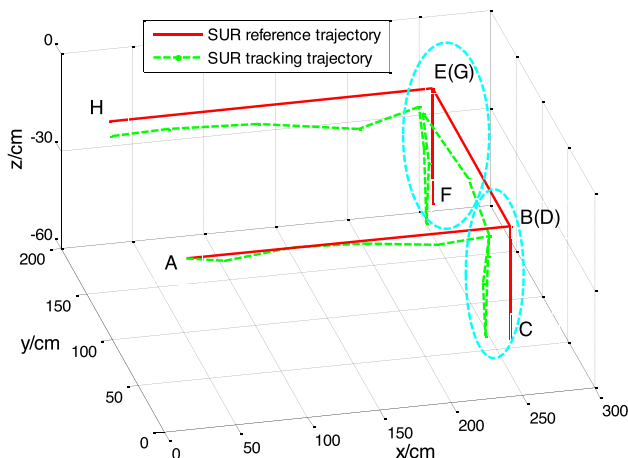


Fig. 11 Path-following results with static obstacle (S2, S3) and moving obstacle (D1); Among them, point Q and R represent the starting position and target position of the moving obstacle, respectively

Table 2 Specification of the SUR

Items	Characteristics
Total mass	Approx. 7.9 kg
Drive mode	Multi-mode (water-jet mode, propeller mode and hybrid propulsion mode)
Attitude sensor	MPU-9250, 15 mm×25 mm, with (3-Axis Gyro, 3-Axis Accelerator, 3-Axis Magnetometer)
Depth sensor	ADPW11 (Panasonic)
Onboard controller	Arduino mega 2560, Steering gear controller
Communication module	Micron data modem (Tritech)

**Fig. 12** Tracking reference path for SUR in real 3D environment, the total time is 34 s (a–h), from the initial position A to the target position.**Fig. 13** Tracking results of the SUR in real environment

5.3 Avoiding Static and Moving Obstacle Experiments

Then, the SUR tracks the reference path in presence of static and moving obstacles, as shown in Fig. 14. Due to

limit of the size of the pool, this paper mainly validates the performance of avoiding obstacles in horizontal plane. Two stationary obstacles (OS 1 and OS 2) with a diameter of 0.1 m and one moving obstacle (OM 1) with a diameter of 0.35 m were placed at the reference path.

First, the SUR starts from the starting point, see Fig. 14a, and follows the reference trajectory. When the OM 1 is detected, the obstacle avoidance on the horizontal plane will be triggered, see Fig. 14c. When the obstacle is bypassed, the SUR will track reference path continually. Then, when the OS 1 and OS 2 are detected, the obstacle avoidance will be triggered, see Fig. 14f, i. About 39 s, the SUR reaches the target point.

The tracking trajectory of the SUR is shown in Fig. 15. As can be seen that the SUR can bypass the obstacles successfully. O1, O2 and O3 indicates the moment when the SUR is avoiding obstacles. After avoiding obstacles, the robot can rapidly follow the reference path.

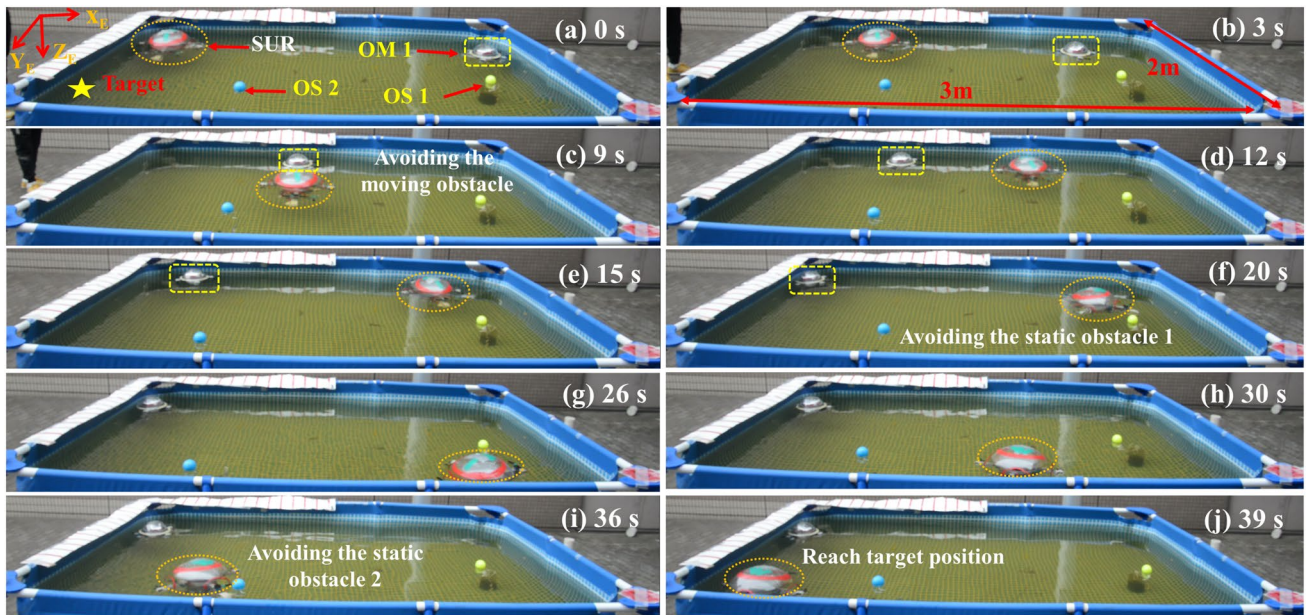


Fig. 14 The movement process of the SUR when there is static and moving obstacles; **a–j** the total time is 39 s, among them, **a–d** are the process of avoiding moving obstacle, and **e–j** are the process of avoiding static obstacles

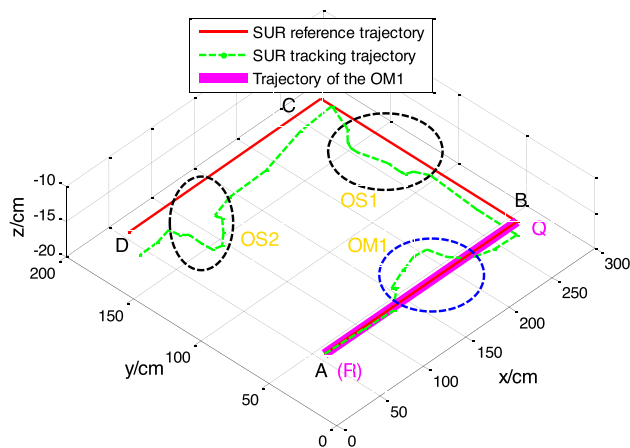


Fig. 15 Trajectory tracking result of SUR in presence of static and moving obstacles

6 Discussion

The SUR can converge to the reference path after avoiding obstacles, to further verify the performance of the SMC–APF, the tracking error is further analyzed.

In Sect. 4.2, the SUR response to the reference path is successful considering the mentioned disturbances and uncertainties. The reference path is determined by the waypoints. To more intuitively reflect the performance of the SMC–APF, the workspace error is calculated, as shown in Fig. 16. It can be seen that the related error of the SMC–APF is 0.08 m, which further verifies that the

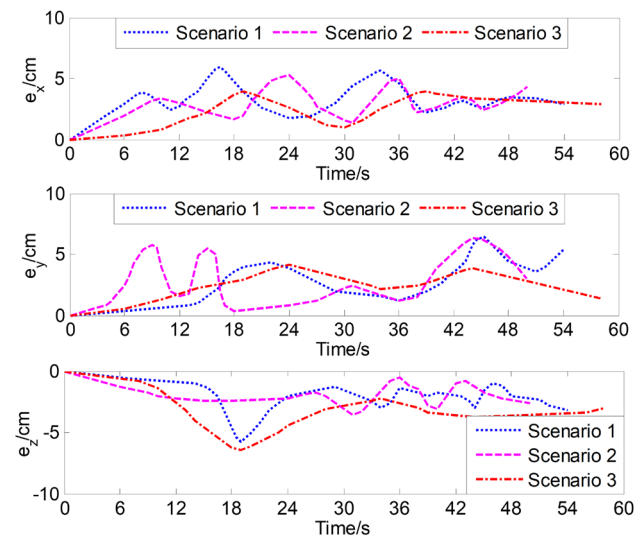


Fig. 16 Position tracking errors for the simulation in tracking experiment (Scenario 1, see Fig. 7), avoiding static obstacle (Scenario 2, see Fig. 9) and moving obstacle (Scenario 3, see Fig. 11)

SMC–APF provides accurate and stable tracking for SUR. In addition, the simulation results show that the SMC–APF always ensures the tracking error converge to an arbitrarily small neighborhood of zero, have a small position error. Noted that, when there is no obstacle, the SUR tracks the reference trajectory, and the position error is less than 0.05 m, which further verifies that SUR has excellent tracking performance. After adding obstacles, SUR can follow the path safely, the maximum position error is less than 0.08 m, and the tracking curve has good convergence.

To sum up, the SUR can quickly follow the safe path after avoiding obstacles. These simulation results validate the strong robustness, high efficiency, effectiveness and stability of the SMC-APF, which provides the solution method for further applications in reality.

In addition, we analyzed the repulsive force performance of the SMC-APF method (see Figs. 9 and 11), from Waypoint A to Waypoint F. It can be seen that when encountering static and moving obstacles, the repulsive force of the obstacles will help the SUR to avoid the obstacles effectively, which is determined by the synthetic force of the obstacle repulsion force and the target attractive force. Compared with static obstacle avoidance, the deviation of dynamic obstacle avoidance from the reference trajectory is larger, but less than 2.5 cm, and larger amount of control effort is required to bypass moving obstacle to ensure the smoothness and stability of the SMC-APF.

In Sect. 5, the SUR can successfully track the reference path and avoid obstacles. To further verify the performance of the SMC-APF, a series of comparative experiments are performed. In [1], An et al. completed obstacle avoidance experiments in a pool (with an area of $300\text{ cm} \times 200\text{ cm} \times 100\text{ cm}$). We set up a stationary obstacle (OS1) in the single obstacle avoidance experiment. The SUR starts from the starting position, time = 0 s, see Fig. 17. It takes about 13 s for SUR to complete the tracking mission using the SMC-APF. The time was optimized for about 1 s. In [2], Li et al. performed obstacle avoidance experiments in a pool (with an area of $250\text{ cm} \times 200\text{ cm} \times 90\text{ cm}$). Mentioned in [2] that the robot tracking error is stable within 0.1 m in a series of experiments. Thus, we calculate the coordinate error, see Fig. 18b, which is stable within 5 cm compared to the ideal trajectory. Considering that the error of the sensor in water is less than 0.2 cm, the dynamic response is strong, and the measurement accuracy is high, the error

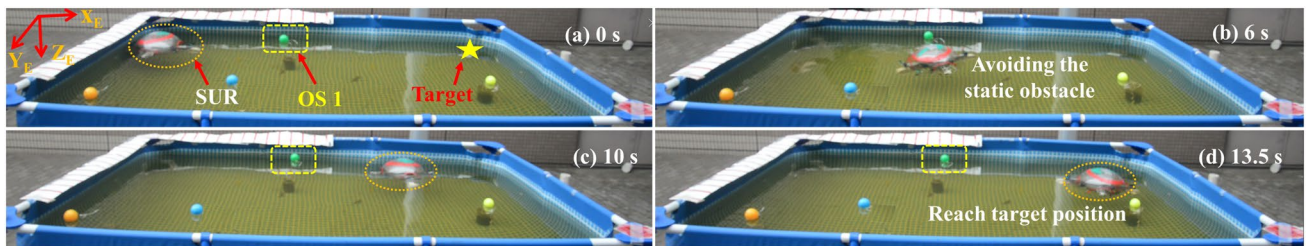


Fig. 17 The movement process of the SUR when there is static obstacle, compared with [1, 2]; From **a–d**, the total time is 13.5 s

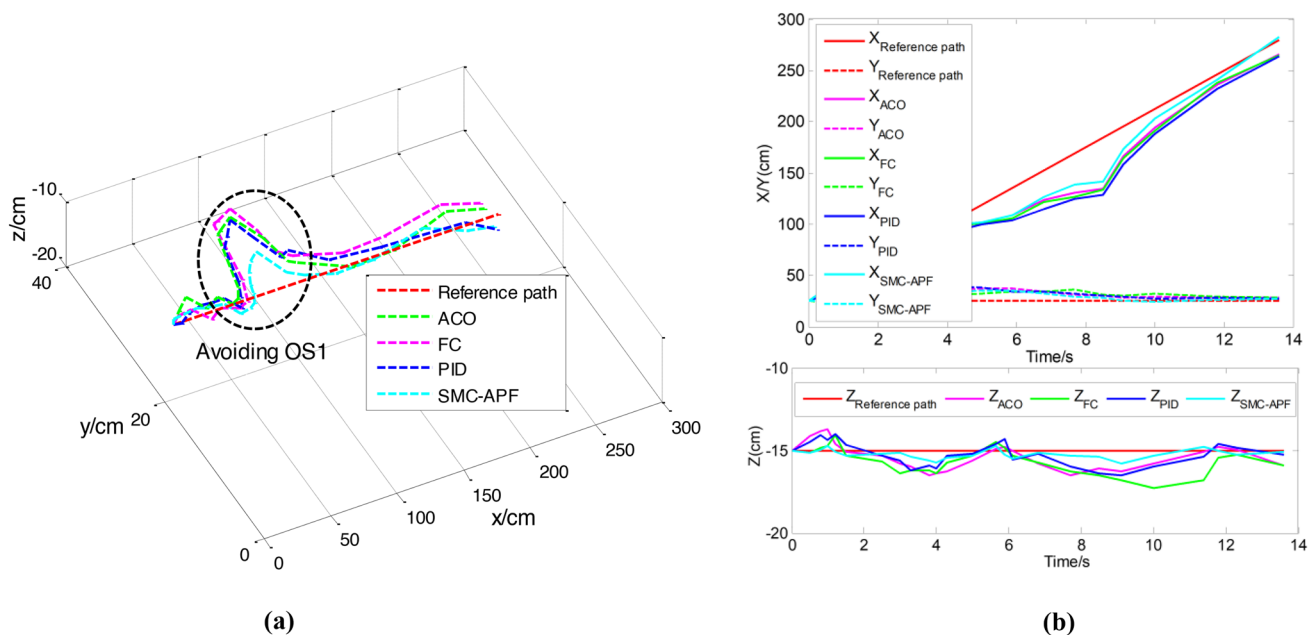


Fig. 18 Trajectory tracking result of SUR in presence of static obstacles, compared the SMC-APF with previous research methods, including ACO [1], FC [2], and PID [26] methods. **a** Results in 3D coordinates; **b** Results in 2D coordinates

Table 3 Results of comparative experiments with previous research methods, including FC, PID and ACO methods

Control method	ACO	FC	PID	SMC–APF
Length (cm)	362	358	374	309
Time (s)	21	19	23	16
Maximum error (cm)	9.45	8.56	9.78	5.63

caused by the sensor is ignored in the error analysis. Of course, due to different experimental conditions, there may be some deviations, which will not be refuted. Furthermore, we compare the SMC–APF with previous research methods, including FC [2], proportional–integral–derivative (PID) [26], and ant colony control (ACO) [1] methods. The initial position is (0.25 m, 0.25 m, − 0.15 m) and the target position is (2.75 m, 0.25 m, − 0.15 m). The length of the desired path is about 250 cm. The trajectory tracking result using SUR under four different methods are shown in Fig. 18. It can be seen that compared with the previous three methods, the SMC–APF has better tracking performance, and the tracking error is reduced by about 3.54 ± 0.61 cm. It can be seen that the SMC–APF can converge better than the FC, ACO and PID methods, which can quickly converge after avoiding the obstacle and track the desired trajectory. Table 3 analyzes and calculates from the three perspectives of length, tracking time and error. It can be seen that compared with the other three methods, the performance is better, namely, the time is more optimized, and the error is smaller. In summary, the SMC–APF has further improved the obstacle avoidance performance of SUR, and in future work, we will further test it in multi-robot coordinative working.

7 Conclusions and Future Work

A path-following strategy was proposed for bioinspired SUR in the presence of obstacles. First, the kinematic and dynamic model of SUR was extracted. Then, guidance and obstacle avoidance laws were developed to track the trajectory safely and quickly. The Lyapunov theory and SMC method were implemented and analyzed, which validated the stability and robustness of proposed control strategy (SMC–APF). Afterward, the capability of real-time performance, such as bypassing static or moving obstacles was verified using APF. Next, based on the proposed control scheme, a series of experimental scenarios were designed using Webots, including path following, static and moving obstacle avoidance, etc. Furthermore, the tracking and avoiding obstacle experiments in uncertain moving obstacle were conducted. Compared with [1, 2], both the tracking error and time were optimized, it could be seen that the proposed adaptive law solved the dynamic uncertainties

and disturbances effectively. As a result, by the aid of the proposed strategy, the stability and accuracy of the SUR could be guaranteed using ultrasonic sensor, and the obstacles could be successfully avoided in an adaptive manner. In the future, we will apply the proposed control strategy for underwater missions.

Acknowledgements This work is supported in part by the National Natural Science Foundation of China under Grant 61703305, in part by the National High Tech. Research and Development Program (863 Program) of China under Grant 2015AA043202, in part by the Japan Society for the Promotion of Science (SPS) KAKENHI under Grant 15K2120, in part by the Key Research Program of the Natural Science Foundation of Tianjin under Grant 18JCZDJC38500, in part by the Innovative Cooperation Project of Tianjin Scientific and Technological Support under Grant 18PTZWHZ00090, and in part by the China Scholarship Council (CSC) for his doctoral research at Kagawa University under Grant 202208050040.

Data Availability Statement All data analyzed during this study is included in this paper. The tracking and obstacle avoidance experiments were performed in simulation and real environment by analyzing the robot attitude and ultrasonic sensor data, as detailed in the graphs in the paper.

Declarations

Conflict of Interest We declare that we have no financial and personal relationships with other people or organizations that can inappropriately influence the work reported in this paper.

References

1. An, R. C., Guo, S. X., Zheng, L., Hirata, H., & Gu, S. X. (2022). Uncertain moving obstacles avoiding method in 3D arbitrary path planning for a spherical underwater robot. *Robotics and Autonomous Systems*, 151, 104011. <https://doi.org/10.1016/j.robot.2021.104011>
2. Guo, J., Li, C. Y., & Guo, S. X. (2020). Path optimization method for the spherical underwater robot in unknown environment. *Journal of Bionic Engineering*, 17, 944–958. <https://doi.org/10.1007/s42235-020-0079-3>
3. Thanh, P. N. N., Tam, P. M., & Anh, H. P. H. (2021). A new approach for three-dimensional trajectory tracking control of under-actuated AUVs with model uncertainties. *Ocean Engineering*, 228, 108951. <https://doi.org/10.1016/j.oceaneng.2021.108951>
4. Kularatne, D., Bhattacharya, S., & Hsieh, M. A. (2018). Going with the flow: a graph based approach to optimal path planning in general flows. *Autonomous Robots*, 42, 1369–1387. <https://doi.org/10.1007/s10514-018-9741-6>
5. Montiel, O., Orozco-Rosas, U., & Sepúlveda, R. (2015). Path planning for mobile robots using bacterial potential field for avoiding static and dynamic obstacles. *Expert Systems with Applications*, 42, 5177–5191.
6. Qiao, L., & Zhang, W. D. (2020). Trajectory tracking control of AUVs via adaptive fast nonsingular integral terminal sliding mode control. *IEEE Transactions on Industrial Informatics*, 16, 1248–1258. <https://doi.org/10.1109/TII.2019.2949007>
7. Guo, J., Li, C. Y., & Guo, S. X. (2020). A novel step optimal path planning algorithm for the spherical mobile robot based on fuzzy

- control. *IEEE Access*, 8, 1394–1405. <https://doi.org/10.1109/ACCESS.2019.2962074>
8. Ji, J., Khajepour, A., Melek, W. W., & Huang, Y. J. (2017). Path planning and tracking for vehicle collision avoidance based on model predictive control with multiconstraints. *IEEE Transactions on Vehicular Technology*, 66, 952–964. <https://doi.org/10.1109/TVT.2016.2555853>
9. Lalish, E., & Morgansen, K. A. (2012). Distributed reactive collision avoidance. *Autonomous Robots*, 32, 207–226. <https://doi.org/10.1007/s10514-011-9267-7>
10. Shen, C., Shi, Y., & Buckham, B. (2019). Path-following control of an AUV: A multiobjective model predictive control approach. *IEEE Transactions on Control Systems Technology*, 27, 1334–1342. <https://doi.org/10.1109/TCST.2018.2789440>
11. Shen, C., Shi, Y., & Buckham, B. (2018). Trajectory tracking control of an autonomous underwater vehicle using Lyapunov-based model predictive control. *IEEE Transactions on Industrial Electronics*, 65, 5796–5805. <https://doi.org/10.1109/TIE.2017.2779442>
12. Khalaji, A. K., & Tourajizadeh, H. (2020). Nonlinear lyapunov based control of an underwater vehicle in presence of uncertainties and obstacles. *Ocean Engineering*, 198, 106998. <https://doi.org/10.1016/j.oceaneng.2020.106998>
13. Liu, J. Y., Zhao, M., & Qiao, L. (2022). Adaptive barrier Lyapunov function-based obstacle avoidance control for an autonomous underwater vehicle with multiple static and moving obstacles. *Ocean Engineering*, 243, 110303. <https://doi.org/10.1016/j.oceaneng.2021.110303>
14. Li, D. L., Wang, P., & Du, L. (2018). Path planning technologies for autonomous underwater vehicles-a review. *IEEE Access*, 7, 9745–9768. <https://doi.org/10.1109/ACCESS.2018.2888617>
15. Molinos, E. J., Llamazares, A., & Ocaña, M. (2019). Dynamic window-based approaches for avoiding obstacles in moving. *Robotics and Autonomous Systems*, 118, 112–130. <https://doi.org/10.1016/j.robot.2019.05.003>
16. Shi, L. W., Hu, Y., Su, S., Guo, S. X., Xing, H. M., Hou, X. H., Liu, Y., Chen, Z., Li, Z., & Xia, D. B. (2020). A fuzzy PID algorithm for a novel miniature spherical robots with three-dimensional underwater motion control. *Journal of Bionic Engineering*, 17, 959–969. <https://doi.org/10.1007/s42235-020-0087-3>
17. Cai, W. Y., Wu, Y., & Zhang, M. Y. (2020). Three-dimensional obstacle avoidance for autonomous underwater robot. *IEEE Sensors Letters*, 4, 7004004. <https://doi.org/10.1109/LENS.2020.3034309>
18. Zhang, S., Dong, Y. T., Ouyang, Y. C., Yin, Z., & Peng, K. X. (2018). Adaptive neural control for robotic manipulators with output constraints and uncertainties. *IEEE Transactions on Neural Networks and Learning Systems*, 29, 5554–5564. <https://doi.org/10.1109/TNNLS.2018.2803827>
19. Yan, Z. P., Li, J. Y., Wu, Y., & Zhang, G. S. (2019). A real-time path planning algorithm for AUV in unknown underwater environment based on combining PSO and waypoint guidance. *Sensors*, 19, 20. <https://doi.org/10.3390/s19010020>
20. Li, Y. X., Guo, S. X., & Wang, Y. (2017). Design and characteristics evaluation of a novel spherical underwater robot. *Robotics and Autonomous Systems*, 94, 61–74. <https://doi.org/10.1016/j.robot.2017.03.014>
21. Yue, C. F., Guo, S. X., Li, M. X., Li, Y. X., Hirata, H., & Ishihara, H. (2015). Mechatronic system and experiments of a spherical underwater robot: SUR-II. *Journal of Intelligent & Robotic Systems*, 80, 325–340. <https://doi.org/10.1007/s10846-015-0177-3>
22. Li, Y. X., Guo, S. X., & Yue, C. F. (2015). Preliminary concept of a novel spherical underwater robot. *International Journal of Mechatronics and Automation*, 5, 11–21.
23. Gu, S. X., & Guo, S. X. (2017). Performance evaluation of a novel propulsion system for the spherical underwater robot (SURIII). *Applied Sciences*, 7, 1196. <https://doi.org/10.3390/app7111196>
24. Gu, S. X., Guo, S. X., & Zheng, L. (2020). A highly stable and efficient spherical underwater robot with hybrid propulsion devices. *Autonomous Robots*, 44, 759–771. <https://doi.org/10.1007/s10514-019-09895-8>
25. An, R. C., Guo, S. X., Yu, Y. H., Li, C. Y., & Awa, T. (2022). Task planning and collaboration of jellyfish-inspired multiple spherical underwater robots. *Journal of Bionic Engineering*, 19, 643–656. <https://doi.org/10.1007/s42235-022-00164-6>
26. An, R. C., Guo, S. X., Yu, Y. H., Li, C. Y., & Awa, T. (2021). Multiple bio-inspired father-son underwater robot for underwater target object acquisition and identification. *Micromachines*, 13, 25. <https://doi.org/10.3390/mi13010025>
27. Ji, Y., Guo, S., Wang, F., Guo, J., Wei, W., & Wang, Y. (2013). Nonlinear path following for water-jet-based spherical underwater vehicles. *IEEE International Conference on Robotics and Biomimetics (ROBIO)*. <https://doi.org/10.1109/ROBIO.2013.6739593>
28. Guo, S. X., He, Y. L., Shi, L. W., Pan, S. W., Xiao, R., Tang, K., & Guo, P. (2018). Modeling and experimental evaluation of an improved amphibious robot with compact structure. *Robot and Computer-Integrated Manufacturing*, 51, 37–52. <https://doi.org/10.1016/j.rcim.2017.11.009>
29. Ma, Y. N., Gong, Y. J., Xiao, C. F., Gao, Y., & Zhang, J. (2019). Path planning for autonomous underwater vehicles: An ant colony algorithm incorporating alarm pheromone. *IEEE Transactions on Vehicular Technology*, 68, 141–154. <https://doi.org/10.1109/TVT.2018.2882130>
30. Wang, J. Q., Wang, C., Wei, Y. J., & Zhang, C. J. (2019). Command filter based adaptive neural trajectory tracking control of an underactuated underwater vehicle in three-dimensional space. *Ocean Engineering*, 180, 175–186. <https://doi.org/10.1016/j.oceaneng.2019.03.061>
31. Bakdi, A., Hentout, A., Boutami, H., Maoudj, A., Hachour, O., & Bouzouia, B. (2017). Optimal path planning and execution for mobile robots using genetic algorithm and adaptive fuzzy-logic control. *Robotics and Autonomous Systems*, 89, 95–109. <https://doi.org/10.1016/j.robot.2016.12.008>
32. Xing, H. M., Shi, L. W., Tang, K., Guo, S. X., Hou, X. H., Liu, Y., Liu, H. K., & Hu, Y. (2019). Robust RGB-D camera and IMU fusion-based cooperative and relative close-range localization for multiple turtle-inspired amphibious spherical robots. *Journal of Bionic Engineering*, 16, 442–454. <https://doi.org/10.1007/s42235-019-0036-1>
33. Mohanan, M. G., & Salgoankar, A. (2018). A survey of robotic motion planning in dynamic environments. *Robotics and Autonomous Systems*, 100, 171–185. <https://doi.org/10.1016/j.robot.2017.10.011>
34. Braginsky, B., & Guterman, H. (2016). Obstacle avoidance approaches for autonomous underwater vehicle: Simulation and experimental results. *IEEE Journal of Oceanic Engineering*, 41, 1–11. <https://doi.org/10.1109/JOE.2015.2506204>
35. Zhang, G. Q., & Zhang, X. K. (2016). Practical robust neural path following control for underactuated marine vessels with actuators uncertainties. *Asian Journal of Control*, 19, 173–187. <https://doi.org/10.1002/asjc.1345>
36. Zhao, Y. J., Qi, X., Ma, Y., Li, Z. X., Malekian, R., & Sotelo, M. A. (2021). Path following optimization for an underactuated USV using smoothly-convergent deep reinforcement learning. *IEEE Transactions on Intelligent Transportation Systems*, 10, 6208–6220. <https://doi.org/10.1109/TITS.2020.2989352>

Springer Nature or its licensor holds exclusive rights to this article under a publishing agreement with the author(s) or other rightsholder(s); author self-archiving of the accepted manuscript version of this article is solely governed by the terms of such publishing agreement and applicable law.